2069 Bhadra (Regular)

1. Forward difference table

t(x)	1	2	3	4	5	6
100		3	28	65	126	217

x	t(x)	F.F.D.	SED	T.F.D.	F.F.D.
1 2 3 4 5 6	2 9 28 65 126 217	7 19 37 61 91	12 18 24 30	6	0 0

a. Explain the mechanism of finding a real root of a non-linear equation using secant method.

Ans:

this method is an improvement over the method of false position as it does not require the conduction f(x0) 4(x1) <0 of the method. Here, also the graph of the function y = f(x) is approximated by a secant line but at each iteration, two most recent approximations to the root are used to find the next approximation. Also it is not necessary that the interval must contain the root.

Taking xo, x, as the initials limit & of the interval, we write the equation of the chord joining these as,

then the abscissa of the pt. where it crosses the x-axis (y=0) in given by

x2=x1- x1-x0 . +(x1)

which is an approximation to the root. The general formula for successive approximation is given by,

$$\chi_{n+1} = \chi_n - \frac{\chi_n - \chi_{n-1}}{f(\chi_{n})} + f(\chi_{n}), n \ge 1.$$

3. Find a root of ex = 32 using bisection method and Newton's Raphson method correct upto 3 decimal places.

of: Let. +(x) = ex-32 (Bisechium Method)

X	0	T
fix)	T	-0.281

It has between 0 & J.

x	0.1	0.2	0.3	0.4	0.5	0.6	0.2
+(x)	0.802	0.6214	0.4499	0.2918	0.1487	0-022)	-0.0862

: + (0.6) is +ve & + (0.7) is -ve.

Let the initial interval (a,b) = (0.6,0.7)

			The same of
a"	643	c= a+b/2	f (c)
0.6	0.7	0.65	-0.0345
0.6	0.65	0.6250	-0.0068
06	0.625	0.6125	0.0075
0.6125	0.625	0.6188	0.0004
0 6188	0.625	6.6219	-0.0032
0.6188	0.6219	0.6204	-0.0015
0.6189	0.6204	0.6196	-0.0006
0 6188	0.6196	0 6192	-0.0002
0-6188	0.6192	0 619 0	0.0001
0.6190	0.6192	0.6191	0.0000

The required real root of ex-32 is 0.6191

nd ses.

2862

Newton Raphson Method

$$f(x) = e^{x} - 3x$$

 $f'(x) = e^{x} - 3$

Iteration formula,

$$t_{new} = \tau_0 - \frac{t(\tau)}{t'(\tau)}$$

= $\tau_0 - \frac{e^{\tau} - 3\tau}{e^{\tau} - 3}$

Determination of initial guess

Hence, the required real root of ex-3x is 0.619)

4. solve vong Gauss Fumination Method:

Sol=: The given bystem is
$$AX = B$$
where, $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 5 \\ 2 & -1 & 3 \end{bmatrix} X = \begin{bmatrix} \chi \\ y \\ z \end{bmatrix}$
 $B = \begin{bmatrix} 6 \\ 10 \\ 4 \end{bmatrix}$

The augmented matrix form is [A/B]

$$\begin{bmatrix}
1 & 2 & 3 & | & 6 \\
2 & 3 & 5 & | & 10 \\
2 & -1 & 3 & | & 4
\end{bmatrix}$$

$$\begin{bmatrix}
1 & 2 & 3 & 6 \\
0 & -1 & -1 & -2 \\
0 & -5 & -3 & -8
\end{bmatrix}$$

$$50$$
, $y=1$
 $47=6-2y-3z$
 $=6-2-3$

5. Write pseudocode to solve a system of unear equation of in unknowns using Gauss-Jordan method.

Ams: Pseudocode:

- 1. Normalize the first equation by dividing it by it, pivot element.
- 2. Eliminate x, term from all the other equations.
- 3. Now. normalize the second equation by dividing it by its pivot element
- 4. Eliminate X2 from all the equation, above and below the normalized pivotal equation.
- 5. Repeat this process until Xn is obminated from all but the last equation.
- 6. The resultant b vector is the solution vector.
- 6. Use lagrange method to find f (2.5) from the following data.

TX	1	2	4		7
もして	1	1-414	1.732	2.00	2.6

$$L_{0}(x) = \frac{(x-x_{1})(x-x_{2})(x-x_{3})(x-x_{4})}{(x_{0}-x_{1})(x_{0}-x_{2})(x_{1}-x_{3})(x_{0}-x_{4})}$$

$$l_0(2.5) = \frac{(2.5-2)(2.5-4)(2.5-5)(2.5-7)}{(1-2)(1-4)(1-5)(1-7)}$$

$$L_{1}(25) = \frac{(2.5-1)(2.5-4)(2.5-5)(2.5-7)}{(2-1)(2-4)(2-5)(2-7)} = \frac{27}{32}$$

$$\frac{1}{(2-7_0)} \frac{1}{(2-7_1)} \frac{1}{(2-7_1)}$$

7. Fit the following set of dato to a curre of the form y = gebit from the tollowing observation by least square method.

[x]]	2	3	4	5	G
x 1.	6.5	9.4	15.2	30-6	49.8

501º:

7:	x; 2	71:71
5.5	1	5.5
65	4	13
9.4	9	28.2
15.2	16	60.8
30-6	25	153
49.8	36	298.8
至4:= 117	Ex; = 91	E1141 = 559.3
	5·5 6·5 9·4 15·2 30·6 49·8	5.5 1 65 4 9.4 9 15.2 16 30.6 25 49.8 36

$$\begin{bmatrix} 0 & \Sigma x_1 \\ \Sigma x_1 & \Sigma x_1^2 \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} = \begin{bmatrix} \Sigma y_1 \\ \Sigma x_1 y_1 \end{bmatrix}$$

$$\begin{bmatrix} 6 & 21 \\ 21 & 91 \end{bmatrix} \begin{bmatrix} 9 \\ 6 \end{bmatrix} = \begin{bmatrix} 117 \\ 559.3 \end{bmatrix}$$

$$6a + 21b = 117 - 0$$
 $21a + 91b = 559.3 - 0$

$$21a + 91b = 5550$$

On solving, $a = -10.46$; $b = 8.56$
 $y = ae = -10.46e$
 $y = -10.46e$
 $y = -10.46e$

8. Derive the expression of simpson's 1/3 rule for integration.

Awa:

Here the total integral is further divided into a equal interval and a must be even.

T =
$$\int_{1}^{4} \frac{1}{2} dt + \int_{1}^{4} \frac{1}{2} dt + \dots + \frac{1}{2} \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2$$

9. Evaluate $\int_{1}^{2} e^{-\tau^{2}} d\tau$ using Romberg method correct upto 3 decimal places.

sof:

Taking h=0.5, 0.25 & 0.125 successively, let us evaluate the given integral by Trapezoidal rule.

1) when h=0.5, the values of y=e-x2 are

$$T_1 = \frac{0.5}{2} \left[(0.3679 + 0.0183) + (2* 0.1054) \right]$$

$$= 0.1493$$

(i) when
$$h=0.25$$
, the values of $y=e^{-x^2}$ are,

 $\frac{1}{x} = \frac{0.25}{2} \left[0.3679 + 0.0183 \right] + 2 \left[0.2096 + 0.1054 + 0.0468 \right]$
 $12 = \frac{0.25}{2} \left[(0.3679 + 0.0183) + 2 \left[0.2096 + 0.1054 + 0.0468 \right] \right]$
 $= 0.1387$

(ii) when $h = 0.125$ the values of $y=e^{-T^2}$ are,

 $\frac{1}{x} = \frac{1.125}{2} \left[1.25 \right] \frac{1.375}{1.375} \frac{1.5}{1.5} \frac{1.625}{1.625} \frac{1.375}{1.625} \frac{1.875}{1.625} \frac{2}{1.875} \frac{2}{1.625} \right]$
 $\frac{1}{3} = \frac{0.125}{2} \left[0.3679 + 0.0183 \right] + 2 \left[0.2121 + 0.7096 + 0.151 + 0.1054 + 0.0713 + 0.0468 + 0.0297 \right]$
 $= 0.1361$

Vang Romberg's formula,

 $1 = \frac{1}{3} \left[1_2 - \frac{1}{3} \right]$
 $= 0.1352$
 $\frac{1}{3} = \frac{1}{3} \left[\frac{1}{3} - \frac{2}{3} \right]$
 $= 0.1361 + \frac{1}{3} \left[0.1361 - 0.1387 \right]$

= 0.1352

10. Solve:

y" + xy' + y = 0; y(0) = 1; y'(0) = 0 for z = 0(01)0.2

Using Ex2 method.

sol=:

Given,

$$y'' + xy' + y = 0$$
 $x_0 = 0$ $x_1 = 0.1$
 $y(0) = 1 = y_0$ $y'(0) = 0 = 70$
Let $y' = 2$ then,
 $z'(7, y, 7) = y''$

Here, f,(x,y,z)=y'=z - (12+y) - 0 f, (1,y,z)=z'=-(12+y) - 0

Now, using R K2 Method for finding y, & Z,

K, = h x f, (x0, y0, z0) ; l, = h x fe (x0, y0, z0)

=0.1 x f, (0, 1, 0) =0.1 x [-0 *0-1]

=0.1 x [-0 *0-1]

12= h* 12 (20+ h; y0+ K1, 20+ l2) =0.1 * 1, (0.1, 1, -0.1) =0.1* [-(0.1* (0.1)+1)] = -0.099

$$K_{2} = h * t_{1} (7_{0} + h_{1}, 5_{0} + k_{1}, 7_{0} + 1_{1})$$

$$= 0.1 * t_{1} (0.1, 1, -0.1)$$

$$= -0.01$$

$$= -0.005$$

$$= -0.005$$

$$= -0.0395$$

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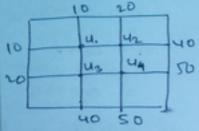
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an) solve the elliptical equation Una + Uyy = 0 for the following square mesh with boundary conditions as shown in the figure below:



44= (100 +42+ 43)/4)

8015

Here, To get the withal values of U_1, U_2, U_3, V_4 where assume that $U_4 = 0$ so, $U_1 = (20+20)/4 = 40/4 = 10$ [Bra. formula] $U_2 = (20+10+0+40)/4 = 17.5 \times 18$ $U_3 = (10+20+40+0)/4 \times 18$ $U_4 = (18+18+50+50)/4 = 34$ $U_4 = (18+18+50+50)/4 = 34$ Now, using Gauss-seidal for successive iteration: $U_1 = (20+42+43)/4$ $U_2 = (60+41+42)/4$ $U_3 = (60+41+42)/4$

u.	U2	43	Uy
14	27	27	38.5
18.5	29.250	29.250	39.625
19.625	29.813	29.813	39.906
19.906	29.953	29.953	39.977
19.977	29.988	29.988	39.994
	29.997	29.997	39.999
19.994	29.999	29.999	40
19.999	30	80	40
20		30	40
20	30		70

2069 Poush (Rock) https://civinnovate.com/civil-engineering-notes/

1. Write an algorithm to find a real root of a non-linear equation using the bisection method.

Aws:

- 1. Decide initial values for 1, and 12 and stopping criterion . E.
- 2. Compute ti= +(x1) and t2= +(x2)
- 3. It titt2 >0 , 1, and 12 do not bracket any rout and go to step 7; otherwise continue
- 4. Compute X0 = (x, +12)/2 and compute to = + (20)
- 5. It to Xto LO then set 12 = 20

else

set 1, = 20 set fi=fo

6. If absolute value of (12-21)/12 is less than error E, then

root = (1,+12)/2 write the value of root go to step 7

goto step 4

7. Stop

2. How can you obtain a real of a non-linear equation using the secont method? Explain graphically and hence obtain the iteration formula. 1/3(2) {(t)=0

secont method, like the take position and brechon methods, uses two initial state estimates but does not require that they must bracket the root. Here, also the graph of the function y= f(z) in approximated by a secont une but at each iteration, two must recent approximations to the root are used to find the next approximation. Also it is not necessary that the inverval must contain the root.

from similar triangles,
$$\frac{f(x_0)}{x_0-x_2} = \frac{f(x_1)}{x_1-x_2}$$

$$x_2 = \frac{x_0+(x_1)-x_1+(x_0)}{f(x_1)-f(x_0)}$$

In general,

$$x_{n+1} = \frac{x_{n-1} + (x_n) - x_n + (x_{n-1})}{+ (x_n) - + (x_{n-1})}$$

3. Find the root of the equation $ze^{\chi} - \cos \chi = 0$ using the secant method correct upto 4 decimal places.

$$80|^{2}: \frac{1}{2} | 0 | \frac{1}{2} | \frac{2}{120} | \frac{1}{2} | \frac{1}{120} | \frac{1}{120}$$

Thus,

a	ь	C	+(1)
0.3	0.8	0.4684	-0.1440
0.3	0.4684	0.5281	0.0317
0.5281	0.4684	0.5173	-0.0013
0.5281	0.5173	0.5378	0.0000

.. The root is 0.5178/

$$2+2y - 12z + 8v = 27$$

 $5x + 4y + 7z - 2v = 4$
 $-3z + 7y + 9z + 5v = 11$
 $6z - 12y - 8z + 3v = 49$

Sol=: The augmented matrix is

$$\begin{bmatrix} 1 & 2 & -12 & 8 & 27 \\ 5 & 4 & 7 & -2 & 4 \\ -3 & 7 & 9 & 5 & 11 \\ 6 & -12 & -8 & 3 & 49 \end{bmatrix}$$

Interchanging Ri and Ry

R₂
$$\rightarrow$$
 R₂ - $\frac{1}{6}$ R₁ ; R₃ \rightarrow R₃ + $\frac{1}{2}$ R₁ ; R₄ \rightarrow R₄ - $\frac{1}{6}$ R₁

$$\begin{bmatrix}
6 & -12 & -8 & 3 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & 49 & | & &$$

50,

$$\frac{11319}{338} \times V = 167.4408$$

$$V = 5$$

$$\frac{169}{42} \times \frac{191}{28} = \frac{3203}{84}$$

$$2 = \frac{3203}{84} - \frac{191 \times 5}{28} \times \frac{42}{169} = 1$$

$$|4y + 4| z - 2| = -\frac{221}{6}$$
on
$$|4y = -\frac{221}{6} + \frac{9 \times 5}{2} - \frac{41 \times 1}{3}$$
on
$$|4z - 2|$$

Also, 6x-12y-82+2V=49

on 62 = 43 +12 x (-2) + 8 x 1 #3x5

7 = 3

sh

Can

Hence, 2=3; y=-2; 7=1; V=5

5. Find dominant Ergen value and the corresponding vector of the following matrix using power method.

Sofn: Let the initial guess vector be.

And, let $A = \begin{bmatrix} 1 & 4 & -1 \\ 4 & 2 & 5 \\ -1 & 5 & 10 \end{bmatrix}$

$$A \times_0 = \begin{bmatrix} 4 \\ 11 \\ 14 \end{bmatrix} = 14 \begin{bmatrix} 0.286 \\ 0.786 \\ 1 \end{bmatrix}$$

AX1 = [2.43] = 13.644 [0.178]
13.644] = 13.644

$$AX_{2} = \begin{bmatrix} 1.442 \\ 6.844 \\ 12.652 \end{bmatrix} = 12.652 \begin{bmatrix} 0.114 \\ 0.541 \end{bmatrix}$$

$$AX_{3} = \begin{bmatrix} 1.278 \\ 6.638 \\ 12.591 \end{bmatrix} = 12.591 \begin{bmatrix} 0.102 \\ 0.519 \\ 1 \end{bmatrix}$$

$$AX_{4} = \begin{bmatrix} 1.178 \\ 6.446 \\ 12.493 \end{bmatrix} = 12.493 \begin{bmatrix} 0.094 \\ 0.516 \\ 1 \end{bmatrix}$$

$$AX_{5} = \begin{bmatrix} 1.158 \\ 6.408 \\ 12.496 \end{bmatrix} = 12.486 \begin{bmatrix} 0.093 \\ 0.513 \\ 1 \end{bmatrix}$$

$$AX_{6} = \begin{bmatrix} 1.145 \\ 6.398 \\ 12.472 \end{bmatrix} = 12.472 \begin{bmatrix} 0.092 \\ 0.513 \\ 1 \end{bmatrix}$$

$$AX_{7} = \begin{bmatrix} 1.144 \\ 6.394 \\ 12.473 \end{bmatrix} = 12.473 \begin{bmatrix} 0.092 \\ 0.513 \\ 1 \end{bmatrix}$$

6 Using Lagrange's interpolation formula evaluate \$127.5) from the table.

x	26	27	28	29	30
(x)	3.846	3.704	3.571	3.448	3.333

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$$\int_{U}(x) = \int_{U}(x) + \int_$$

$$\frac{1}{2(27.5)} = \frac{(27.5-26)(27.5-27)(27.5-29)(27.5-39)}{(28-26)(28-27)(28-29)(28-39)}$$

$$= \frac{45}{64}$$

$$\frac{1}{29-26} \left(\frac{27.5-26}{29-27} \right) \left(\frac{27.5-28}{29-26} \right) \left(\frac{27.5-28}{29-26} \right) \left(\frac{29-27}{29-28} \right) \left(\frac{29-30}{29-30} \right)$$

$$= \frac{-5}{20}$$

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$$J_{4}(1) = (1 - 7_{0})(1 - 7_{1})(1 - 7_{2})(1 - 7_{3})$$

$$=\frac{3}{128}$$

7. Using natural cubic spline interpolation technique, estimate the value of y (0.5) from the following data.

X	0		2	3
		2.2	1.0	0.5

Sol=! Here is not equal interval thus we can write,
$$k_{i-1} + 4k_1 + k_{1+1} = \frac{6}{h^2} \left[y_{i-1} - 2y_i + y_{i+1} \right]$$
 we have $h=1$

4									
(8)	The	distan	ce all	braves	sed in	Hne t b	y an 60	ect may	1179
	in a straight line is given below:						9		
		0. 11		0-11/2					
	t(In &	econds)	10.01	01101	2 0.3	0.4 0	2 0.6		
		Hones)		1.5 7.1			7 50.0		
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	0.6	50.0	13.3.	1.1	-0.9	0.1	2.5	8.8	
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	Voing Perstons forward Interpolation formula,								
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		30	a Charles	21		0	ال		
	=14.3 + (+-0.3) 10.2 +1 (+-0.3) (+-0.3-0.1) x 2 +								
	(01) 2(01) (01)								
		13/16/1		. 1 126	3//1-	6.4711-0	5 x /200		
				1 6.0	-)(-	8.4) (F-0	1 (100)		

```
01, 4+ = 14.2+ 102(+-013) +100(+-0.3)(+-0.4)
                                        -150(t-0.3) (t-0.0)(t-0.5)
              2 14.3+ 102 (+0.3) + 100 (+2 -0.7+ +0120)
 150 t3-0.56-0.76 + 0.35+ +0.120+-0.060
                    1=14.3+102+-30.6+100+2-70++12.
                                      - 15063 x 18063 4710.56 x 9
                              4-7-38-St +2202-15062.
      NOW,
         velocity at trossec.
                         256 = +38.5 + 2x230+ - 3x150+2
                                             The state of the s
                                          = - 28.5 4 4x 280x 0.2 - 3x 150x 0.22
                                     11 = 128.5 +112-18 (118 118 118 118 118 118
   Also, actoleration as toossec.
                                                                                         all post good as expensed
                     224 = 2x220 - 3x2 x150x4
                                                        = 560 - 180
```

Evaluate the following coving Gransian & point formula. (0.9) du sisput para (a) produce (a) produces Changing the limit of the integration from (0,2) to (-1,1) 2- 1 (b-a)4+ 1 (b+a) = = (2-0)u+/2(b+a)()' Then, Using browston 3 point formula, we ges 8 x 0777/15 f (-1/3/5) +d (1/3/5)] # 0.637 + 5 0.928 + 0.553 VIVIANIA

https://civinnovate.com/civil-engineering-notes/ save the esdinary differential equations 3"= oig' - 42 for no 0.6 with initial (Condition) (g(0)=1, y(0)=0 by using RK-2 D-10) Method (Take h= 0.3). Per de Contrata Contrata Constitution Sob 42-42 Property of the state of initial condition, milling and 11111 May y(0)=1 4'(0) = 0 1) Vindo Hese, Let y= 2 men y"= z! 11 Nois, g'= = f, (a, y, z) - 0 $y'' = z' = xz^2 - y^2 = f_2(x, y, z) - (y, z)$ 9(0)= 90=1. ; 20=0 g(0)= 210)= 20= Q. h= 0.3. Now wing RK-2 Memor for finding y, &Z, K,= hf, (90, 50, 20) d,= hf2 (90, 50, 30) = 0.3 × f2 (0, 1, 0) K2= nf, (noth, y0+K,) 20+1,) d2= nd2 (0.3) 1, -0.3) = hf, (0.3, 1, -0.3) = 0.3x (-0.973) =-0.292011 = -0.090 ". K = KI + KE -- 0.045 :. L= J, +12 = -0.296.

+ 1-0.045 -0.296. =10:955 M WILL AND MAN GNEAU AU AND A LAN Ke=nf. (0.6,0.866, -0.562) d2=hf2 (0.6,0.866, -0.562) - -0.169 VII VIII -0.168 .. K: KIKK2 1 +0.129 11. (= 1/425 - -0.217 O'IN baste Ascudo-Lode so solve an instal value problem (Hirst Order differential equation) wing the Runge Kutta fourth order Method R-K 4th Ordered Micknod. is most Commonly lesed and is often iseferred ito as Runge - Kulta method only working Rule'-

The steined and 5-point formular for given egit is
4:-15 + 4:+55+ 4:55+1 + 4:55-1 - 44:51 = \$12.27 N/30)
10 mg (m, 3m) 0 100 10
-> 41 + 41 + 4 41 + 441 + 441 - 441 = 2 f(1, 1)
For, each (1); 1(1,2)
(1, 10)
440 Ung + unat us + us - 4us = 2x1x4
0), 0+42+0+43-44, -8
on, u, = (42+43-8)14
For f(1);)=f(2,2)
Us12+ U3,2+ U2,3+ U211-46422 = 274x4
05 41 + 0 + 0+4, -445 = 321
ps, 41+0+0+0+44 - 442 = 321
9, 42= (4,+44-32) 4 +
For ((1,;)= f(1,1)
40, + 42,1+41,0 - 441,1 = 2
0 0 4 4 4 4 0 - 44 2 = 2
10 11 11 13
01, 43= (4,444-2)/4

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   Using + Usin + Usis + Usio - 4 Un = 8xuxi
   or, 43+ 0+ 42+0-444= 8
         er, 44= (42+43-8)/4.
 From eq (19) ((1), coc found )
              91 = 44 = (42+43-8)/4.
   Thus, above eggs reduces to! -! " I I I
    4, = (24, +43-8)4 = (4, -16) 12
     43= (24,-2) 14-(4,-1)/2
    44=41 41:49=0,041=-2
  Let for une mittal values for Gaus- seidal itercition
     Method be 42=0, 42=0, leveletes edele 44
                                         42 43
                                                                                0-1-5
             -2
                                                                               - 2.513
            -4.625
                                          -10:313
            -5.281
                                          -10.641
                                                                               -3.1411
                                                                                - 3.823
            -5.445
                                             -10.723
                                                                                - 3. 243
             -5.486
                                          -10.743
                                                                                                                1. 10 1 10 11 11 11 11 11 11
            -5.497
                                           CD1701-
                                                                                 - 3.249
                                                                                 -3.250
                                           - 10.750
             -5.499
                                                                                    -3.250
            -5.5
                                             -10.750
              -5.5
                                             -10.750
                                                                                -3.250
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Hence,

not done: - 3, 2, 11

		Not o	consi	1 2 1			
0.0	And a aco	a used or	05-3n3-	1=0	Correct 1	up to for	u decin
ARM	al blaces ru	ing the Seco	and Meen	od.			
	Sel						
	Heso Ke	+ f(n) = 25-	328-10	so bu	at flo	1=-184	鱼)= 王
	Taking	rnotial appre	exi mation	MOFO	891=2	8 , 40 e ho	ive.
	2 10 1	0.5 11	1.5	2	Q.5	3	
	few or	0.5 1 1	-3. 501	1	49.781	161	
	The Real Property lies			200		SEPTIME TO	
	Aved Noc	5,					
	T	teration for	mula :			No. of Contract of	
	c= afc	b) - bf(a)					
		(b) - f(a).	9837.98				
	Turially	let a = 03	b = 0.9				
190 9	THE PARTY OF		The last				
	a	Ь	c				
	0.3	0.9.	-0-1263				
	0.9	-0.1263	-0.7629				
	0.1263	-0.7623	-0.7100				
	-0.7629	-0.7190	-0.7415				
	- 0 71 0 -	-0.7415	-0.7413				
	-0.7415	-0.7U()	-0.7418				
	-07413	-0.7419	-0.7418	6 8 10			
	14 On	100	35.00 P. S	22/1/2	78311.9		
VIII.	Hence, whe	in +308	· 8.7418 · /	1.		S. British	
		San N San	SAME BY				
17	RASSING SAC			AST			

	(Newson)
-	a la la to find ou sort of a non- week
(6.5	watte a Beulo-lode to find a cost of a non-Unearly
	rusting Biseation Method.
	1. Decide instead values from X, (M) & stopping Biterion F. d. Compute fi= f(n) & f= f(n).
	1. Decide instal values febs X, (x)
	a compute fi= f(a) & f=f(n2).
	3. If fix fa 70, m, and me alo not bracket any acot and go to step 7.
	and go to step 7.
	4. Compute no= (nit no) la and compute fo=f(no).
	5. of f.xfo20 men.
	I I A CI - O
	else.
	set h = fo
	ger frate of Conna New is less Inon Ever E.
	6. If absolute value of (n2-n1) n2 is less bran enor E
	chen
	2007 - (2, +22) /2
	write une volue quost.
	go to step -7.
	else .
	go to step 4.
	1. stop
0.4	
	swabu éterative memod.
	anty 12- 202-10
	42+02+00 =8
	201+24+2=7
	2+37+22-05-5.
18.1	The second secon
No.	

San
Given Equations are!
ant 4+12- 200=-10
4m+22+ 20=8
87+29+02= 7
9434 +22-10=-5
isjusting the equations in the form of partial
pivoring as:
4n+ RZ+10=8 -
2+34+22-0=-5
3m+24+2z = 7 - 11)
2n+y+z-2w=-10 -
Now, in order do dave mese equations, rue Gours-Seidai
The state of the s
Merrod as:
Merrod as: n = (8-22-w)/4
Merrod as: $n = (8 - 2z - \omega)/4$ $y = (-5 - 2z + \omega)/3$
Merrod as: $n = (8-2z-\omega)/4$ $y = (-5-x-2z+\omega)/3$ z = (7-3x-2y)/2
Merrod as: $n = (8 - 22 - \omega)/4$ $y = (-5 - 22 + \omega)/3$ z = (7 - 2n - 2y)/2 $\omega = (2x + y + 2 + 2\omega)/2$
Merrod as: $n = (8-2z-\omega)/4$ $y = (-5-9z-2z+\omega)/3$ z = (7-9n-2y)/2 $\omega = (2x+y+z+4\omega)/2$ bow, Let the with a values of zew be die z= $\omega = 0$,
Merrod as: $n = (8-2z-\omega)/4$ $y = (-5-x-2z+\omega)/3$ z = (7-2x-2y)/2 $z = (2x+y+z+2\omega)/2$ bow, Let the frontal values of zew box is $z = \omega = 0$, $z = (2x+y+z+2\omega)/2$
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Merrod as: $n = (8-22-\omega)/4$ $y = (-5-91-22+\omega)/3$ z = (7-9n-2y)/2 $w = (2x + y + 2 + 4\omega)/2$ bow, Let the Probably values of $z + \omega = 0$, $z = (2x + y + 2 + 4\omega)/2$ $z = (2x + y + 2 + 4\omega)/2$
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Method as: $n = (8-2z-\omega)/4$ $y = (-5-x-2z+\omega)/9$ $z = (7x + y + z + 2\omega)/9$ $z = (2x + y + z + 2\omega)/2$ None, Let the trivial values $q = z + z = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + y + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + z + 2\omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + z + \omega)/9$ None, Let the trivial values $q = z + \omega = 0$, $z = (2x + \omega + \omega)/9$ None, Let the trivial values $z = (2x + \omega + \omega)/9$ None, Let the trivial values $z = (2x + \omega + \omega)/9$ No
Method as: $n = (8-2z-\omega)/4$ $y = (-5-2z+\omega)/3$ $z = (7x + y + z + 4\omega)/2$ $z = (2x + y + z + 4\omega)/2$ Now, Let the finitial values of $z + \omega = 0$, $z = (2x + y + z + 4\omega)/2$ Now, Let the finitial values of $z + \omega = 0$, $z = (2x + y + z + 4\omega)/2$ Now, Let the finitial values of $z + \omega = 0$, $z = (2x + y + z + 4\omega)/2$ Now, Let the finitial values of $z + \omega = 0$, $z = (2x + y + z + 4\omega)/2$ $z = (2x + y + z + 4\omega)/2$ Now, Let the finitial values of $z + \omega = 0$, $z = (2x + y + z + 4\omega)/2$ $z = (2x + y + z + 4\omega)/2$ Now, Let the finitial values of $z + \omega = 0$, $z = (2x + y + z + 4\omega)/2$ $z = (2x + y + z + 2\omega)/2$ $z = (2x + y + 2\omega)/2$ $z = (2x + y + 2\omega)/2$ $z = (2x + y + 2\omega)/2$ z =

~	4	2	w	6.83
2	-1.44	3.015	5.531	
-0.410	-1.536	3.299	4,991	
- 0.830	-1.903	2.943	4-622	
- 0.897	-1.879	2.562	4.719	
- 0.627	-1.650	2.539	4.985	
-0.459	-1.520	2.743	5.095	
-0.516	-1.584	2.857	5.004	
70.648	-1.632	2.850	4.884	
- 0.695	-1.723	2.746	4.865	
-0.539	-1.679	2.705	41924	
- 0.593	-1.634	2.741	4.970.	
-0.613	- 1.633	2.786	4.964	
-0.634	-1.658	2.793	4.933	
-0.615	-1.674	2.770	4.918	
- 0.603	-11669	2.753	4.927	
-0.613	-1.657	2.755	4.941	
-0.620	-1.652	2.767	4.044	
-0.621	-1.657	2.773	4-931	
-0.681	-1.662	0.769	4.933	
-0.615	-1.663	2.764	4.933	000
-0.615	-1.660	2.763	4 . 933	
- 0.617	-1.659	2.765	4. 938	
- 0.613	-1.658	2.767	4.937	8 10 14
-0.618	71.660	2.767	4.936	
-0.617	-1.660	2.766	4.925	
- 0.617	-11.6=9	2.765	The second secon	0.01-
-0.617	-1.659	2,766	4.936	
Lience				

2 = - 0.617; y=-1.659; Z= 2.766; W= 4.938

(-5)	and the largest Eigen value & corresponding Rigen Vector
	of the Jollowing Matrix rising power Method.
	[a -1 0]
	0 -1 2.
	Son
	Criven; [a -10]
	Les A= -11 and mital trues vector
	0 -1 2 be X0 - [1] [hen.
	[0 -1 2] he Xo - [1] then,
	Ustra Power Method.
	AX*> Z,> A, X,
	De have,
	AX0= 2-10 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	-1 2 -1 × 1 = 1 0 = 1, ×
	LO -1 2 [1]
	AX,= 2 -1 0 [1]
	0-12 1 = Cax2
	0 -1 2 1
	AV -1 0 1 (-0.75)
	AX2= 0 -1 2 1 = -3 01 = 2xxx
	[-0.750]
	AV =[2 -107 [cd]
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
	0-12 -0750 -0714

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$$AX_{11} = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix} \begin{bmatrix} -0.710 \\ 0 & | = 3.42 \\ 0 & -0.702 \end{bmatrix} \begin{bmatrix} -0.703 \\ 1 & | = \lambda_{S}X_{5} \\ -0.703 \end{bmatrix}$$

$$A \times 6 = \begin{bmatrix} 0 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix} \times \begin{bmatrix} -0.707 \\ 1 \\ -0.707 \end{bmatrix} = 3.415 \begin{bmatrix} -0.707 \\ 1 \\ -0.707 \end{bmatrix} = 1.717$$

Street Xn ~ Know

Thus, dangert Eigen value 1053.414 and largert Eigen. Vector is [0.707].

			nttps://civinr	novate.com	/civil-engir	neering-note	sl	
0.6)	Find	the v	alues of	y out n's	1.6 &	2=4.8	som the Jollon	
8.3	poin	ns rusi	ng Dele	otoris 10	recepora	is on tech	snique.	
		01)	1 2	13	4 9	5	a na	
		9	4 7.5	4	8.5 9	·G-		
	So	5						
		Forco	nd Dil	ference	Table	ا دف ا		
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	n	4	10 mg.	124	134	1 149		
	1	4	1411		14884		(11) priss	
	. 2	7.5	3.5		138 3	Marie Contract		
	4.3	14	-	-7	1			
	4		4.5	8	15	13		
	6	9.6.	1 41	134	:111.5	-26.5.	CI HOLL SO	
	, We	-tarke	240=0					
	A YA				n ord	13 3 4 1		
		ang p	evotoru kor	wasd i	nterporal	n'a formi	va, we get	
	Cen	. 0.1				,		
	Just 1	1001-	x 04(0)	LL - 36 (SAIL	-			
		t 21=	1.4					
							1 Z 1883 FT 3 A	
	P= 2- 20 = 1.6-1 = 0.6							
	50 = 410) - 4 + 000 + 0000 1 1							
	\$ = y(n) = 90+ POYO + P(P-1) D'yo + P(P-1) (P-2) D'yo							
1993	+P(P-D(P-2)(P-3) Mys +.							
				41		0 36 4	1.	
	4(1.6)	=4+0	0.6×3.5+	0.6(0.	(5-1)(1-3	+ 0.6(0.6	-1)(06-2) × 15	
			40.6	(0.6-1)(0.6-5)(0.	(6-3)	20.67	
	4 0.6(0.6-1)(0.6-2)(0.6-3) x(-26-3)							

= 4+21+6.840+-3.360 +0.930 revaluable and the transfer of = 4.470 (1) ot x = 4.8. P= 20-20 = 104.8-1 = +3.8. :-4(4.8)= 4 + 3.9x3.5 + 3.8 (8-1) x (-7) + 3.8 (3.8-1) (28-2) x15 + 2.9 (98-1) (3.8-2) (3.8-3) x (-26.5) = 4 + 13.3 + - 37. 240 to alease - 16.918 + 47.980. = 11.022. Hence, y(1.6) = 4.470 (8.7) Find the curve of the from y= at hichart fits the methos! y 1.2 2.5 6.25 15.75 48.65 Her, Marine

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Ų			dnou	dny:	(In hi) 2	1 (Ina;) (Ina;)
	217		O	0.182	Only	O Marilana
	2	2.5	0.693	0.916	0.480	0.635
	3	6.25	1.095	11833	1-207	12.0313 10
		15:75	1.386	A . 757	1.9322	2-822
	4	28.65.	-	3.355	2:330	2.400
		000				CALL CALL
	Sum	1	4-787	9.045	6.199	11.870: 0001

hen, b= ngloarlayi - gloni glayi, ng (doai)2 - (glani)2

= 5×11.870 - 4.787 × 9.043 5×6.199 - 4.787)2

=1.939.

Also,
dna = 1 (& lny; - b&lnni)

or, dna = = = (9.0813 - 1.093 x 4.787)

Ina - -0.105

i. a = 0.9

parces function as: y= 0.9 x 1.895 for, coc obtain

(8.8)	The follo	prive	habic	gives &	he ang	le in il	ea dian	1 (0) n	20-
	ugh writer in actoring sod has temed for various								
	values of time in seconds (b). And the langular velocity								
	and angular acceleration at to 0.2.								
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9	Evaluate ene. Fritegral I= (10g (21+1) + 8m22) dr.						
	using Gaussian 2. point & s-point grosmules.						
	Given, 1.						
	T= ((0g(n+1)+ 8n2n) dn.						
	Decussion deposine formula: (n=2)						
	I= [log(2+1) + pin22] da						
	= f(-1/3) + f(1/3) [after changing one unos						
	from (0.2, 1.2) -> (-1,1), by,						
	n= 1 (b-a) u+ 1/2 (b+a) Also,						
	= \$(1.2.0.2) u+ 1/2(1.2+0.2) do= 0.5 du.						
	= &u+0.7 => 0.5u+0.7.						
	so (nal, f(u) - log (0.54+0.7) + 8in2 (0.54+0.7) Then,						

Craussian downt formula is given by I = (0.5 f(u) du [auste [log(0.54+0.7) + 81,2(0.54+0.7)]du = 0.5 f(-/v3) + f(/v3) = 0.5 [log(0.5x-1/13+0.7) + 812 [0.5x-1/13+07) } + 2103 (0.5x(W3)+0.7) +8102 (0.5x /3) +0.74 = 0.5 [0.847 + 0.914] Caussian 3-point formula is given by: f(0) = log(0+0.7) ~ 8/n 2(0.7) I= Josf (w) du = 0.5 8 fro) + 5 [f. (- \3/5) + f (\3/5)] =0.5[0.728+5(0.081+0.860)] = 0.630.

0.19	cave me differential equation,
4:16	solve the differential equation,) du = (1+2)/y, whin n <0(0.2) o.4 (y(0)=1
	200
	using RK Um order Method.
	305)
	Convenience Constitution of the Constitution o
	du - (1+22)4
	du - (1+ of) y.
	g(0)=1=40; 20=0, 20=0.4., h=0.2.
	2 10 100 104
	x 0 0.2 0.4 y 1 ? ?
	· · · · · · · · · · · · · · · · · · ·
	1. y(0.2) = ? and y(0.4) ? Now, Applying RK-4 morder Medhod, we have, for, y(0.2) y,
	and the second second
	100, 9(0.5) 8,
	V by C (a u)
	K,=bxf,(20,40) \$1500
	1 . 1/0 4 net
	Va=nf(notoshyo+osk,)
	- 0.0 ((a., 1.) = 4 m 0 000
	= 0.8 f (0.1, 1.1) = decide 0.222
	Va= hf (90+ 0.5h, 40+ 0.5kg)
1000	3 100001, 3000 322)
	= 0.2 f(0.1, to E16) = 0.045.
100	27(01) (446) = 0.00(5.
	Ve = hof (man, cent v)
400	= 0.2 f (0.2, 01.045) = 0.217.
	= 1100) = 0.217.

C. K = K + & X + & X g + K W - 0.2 + 2×0.222 + 2×0.645 + 0.217 = 0.159 . : · y (0.2) = yotk = 1+0.159= 1.159. = y.// Again, (0.4). K,= kf(91341) 2 -0.2 f(0.2 1.159) - 0.241 Ks-hd (2,+0.5h, y, + axxk,) -0.2 f (0.3, 1.280) = 0.279 11 10 has K3 = hf(9, +0.5h, y, +0.5kg) =0.2f(03,1.299) = 0.283. K4- hf(9,+k, 4,+ K3) = 0.2 (0.4, 1.442) = 0.335. : 3 K = K, + 2 X 2 + X X X Y X Y = 0.241 +2x0.279 +2x0.283 +0.335 :. y (04) = 9,+ K + 1.153+0.283 = 1.442 Mence, y, = 1.150 and y2=1.442.

gos the following requare mean with the boundary · 44 42 46 2000 here, First finding the Philial values In the following older, ug=0, 47=0 45= 4 2000 + 1000 + 2000 + 1000 | Stat . formula 41 - 45 0+ 1500 +100+2007 = 2008. [Diag formila] 43 = 4[0+1500+ 2000+1000] = 1125 [Diag. fromula] 47 = 4 [0 + 1500 + 1125 + 0] = 656,25. [Diag. formula 49 = \$ [1000 + 1125+ 1500 + 1125] = 1188 . [stel- fermula] 44 = 4[2000+1188+51125+1125+1500] = 1438 [tod formula].

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r-axis & y-axis.

:. 4, = 43=47=4g= 1125

: · 42-48=1188

:. 44 = a6 = 1438

. · 45 = 1500

wing the wondard formula as;

4 (n+1) = 4[1000+42] + 500 + 414]

4 20+1 = 1/4 [4,0+1 +4,0 + 1000 +45]

48 = 1/4 [2000 +45 + 4, 1 +4, 1]

45 mm) = 1/4 [44 + 44 + 42 + 442].

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